

LECTURE NOTES

Ay/Ge 132

ATOMIC AND MOLECULAR PROCESSES IN ASTRONOMY AND PLANETARY SCIENCE

Geoffrey A. Blake

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Ge 132: *Atomic and Molecular Processes...* by E.F. van Dishoeck, Caltech

Ay 522: *Astronomical Spectroscopy* by J.H. Black, University of Arizona

Ay 209: *Interstellar Medium* by A. Dalgarno, Harvard University

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