Influence of interaction between small asperities on various types of slow earthquakes in a 3-D simulation for a subduction plate boundary

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A B S T R A C T

Recently, the occurrence of slow earthquakes such as low-frequency earthquakes and very low-frequency earthquakes have been recognized at depths of about 30 km in southwest Japan and Cascadia. These slow earthquakes occur sometimes in isolation and sometimes break into chain-reaction, producing tremor that migrates at a speed of about 5–15 km/day and suggesting a strong interaction among nearby small asperities. In this study, we formulate a 3-D subduction plate boundary model with two types of small asperities chained along the trench at the depth of 30 km. Our simulation succeeds in representing various types of slow earthquakes including low-frequency earthquakes and rapid slip velocity in the same asperity, and indicates that interaction between asperities may cause the very low-frequency earthquakes. Our simulation also shows chain reaction along trench with propagation speed that can be made consistent with observations by adjusting model parameters, which suggests that the interactions also explain the observed migration of slow earthquakes.

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1. Introduction

Owing to dense networks of high sensitive seismic stations, low-frequency earthquakes have been detected in the southwestern part of Japan at a depth of about 30 km (Obara, 2002) on the subduction plate boundary (Shelly et al., 2006), where slow slip events also have been detected by GPS networks (Hirose and Obara, 2005), and there are large, strong asperities such as Tokai, Tonankai, Nankai earthquakes on the shallower part of subducting plate boundary above the depth of 30 km (e.g., Obara, 2002). Ito et al. (2007) found that not only low-frequency earthquakes but also very low-frequency earthquakes occur in the same region, and suggested that the asperity size of very low-frequency earthquake is larger than that of low-frequency earthquake. However, it has not been clear from hypocenter determination studies that the locations of low-frequency earthquakes are always different from those of very low-frequency earthquakes. Ide et al. (2007) categorized low-frequency earthquake, very low-frequency earthquake, slow slip event and episodic tremor and slip as a group named “slow earthquakes” with similar scaling relation in different scale of duration time (e.g., slow slip event: several days to years, low-frequency earthquake: several tens of seconds to several days). Since slow slip events are accompanied by low-frequency earthquakes as observed in Bungo channel region, southwest Japan (Hirose and Obara, 2005), slow slip events may be composed of some groups of low-frequency earthquakes and/or very low-frequency earthquakes.

Some low-frequency earthquakes seem to migrate along trench at rates of 5–15 km/day in Cascadia (Rogers and Dragert, 2003) and 10–15 km/day in southwestern Japan (Obara, 2002; Obara and Hirose, 2006); Obara (2002) suggested that this migration is caused by the movement of fluid dehydrated from the slab, but it is still unclear whether fluid flow over several tens of kilometers is a necessary condition for the migration of low-frequency earthquakes.

Slow slip transients and their propagation processes have been explained by numerical simulation studies based on rate- and state-dependent friction laws. Liu and Rice (2005) succeeded in reproducing important aspects of aseismic slip transients, by introducing along-strike variations of constitutive parameters or non-uniform initial conditions to excite the non-uniform slip patterns that are intrinsic to spatially homogeneous fault models with large aspect
ratio (Horowitz and Ruina, 1989; Hirose and Hirahara, 2002). Inhomogeneity of friction parameters may also affect the migration of low-frequency earthquakes. Shibazaki and Shimamoto (2007) represented short-interval slow slip events by considering the frictional behavior of the unstable-stable transition regime at high slip velocity. The friction law has a significant influence on models of slow slip event.

On the other hand, Matsuzawa et al. (2004) proposed that aseismic afterslip is propagated by a chain reaction of rupturing asperities. We suggest that this process may also explain the along-trench propagation of low-frequency earthquakes or very low-frequency earthquakes. In this study, we investigate whether interaction between small asperities along the trench can explain the various types of slow earthquakes and their migration processes by numerical simulations of subduction plate boundary models based on a rate- and state-dependent friction law, comparing our simulation results to other studies.

2. Numerical model

The three-dimensional (3D) numerical simulation employed in the present study is similar to that described by Liu and Rice (2005) and Ariyoshi et al. (2007a). The model considers a planar plate interface dipping at 15°from the free surface in a half-space homogeneous elastic medium (Fig. 1a) with periodic boundary condition along the strike direction. The plate interface is divided into 1024 (strike) × 195 (dip) cells. Slip is assumed to be pure dip and to obey the quasi-static equilibrium between shear and frictional stresses:

\[ \frac{\partial \sigma}{\partial t} = \kappa \left( \frac{u_i}{g} - V_{pl} \right) - \frac{G}{2} \frac{\partial u_i}{\partial t} \tag{1} \]

Here, the subscripts \( i \) and \( j \) denote the location indices of an observation and a source cell, respectively. Eq. (1) describes the stress in the \( i \)-th cell caused by dislocations, where \( V_{pl} \) is the relative speed of the two plates, \( \kappa \) denotes time, \( N \) is the total number of cells, \( G \) is rigidity, \( \beta \) is the shear wave speed, and \( K_\beta \) is the Green’s function for shear stress (Okada, 1992) on the \( i \)-th cell. \( K_\beta \) is calculated from the quasi-static solution for uniform pure dip-slip \( u \) relative to average slip \( V_{pl} \) (Savage, 1985) over a rectangular dislocation in the \( j \)-th cell. The first term of the right-hand side has the form of a convolution. The fast Fourier transform can be used for analysis of the along-strike component because the Green’s function \( K_\beta \) for the strike direction is dependent on the relative distance between the observation and source points (Rice, 1993). The last term in Eq. (1) is introduced to incorporate radiation damping (Rice, 1993).

In Eq. (1), the effective normal stress \( \sigma \) is given by

\[ \sigma_i(\omega) = \kappa(\omega) (\rho_{rock} - \rho_w) g z_i \tag{2} \]

where \( \rho_{rock} \) and \( \rho_w \) are the densities of rock and water, respectively, \( g \) is acceleration due to gravity, and \( z \) is depth. The function \( \kappa(\omega) \) is a super-hydrostatic pore pressure factor as given in Fig. 1b, which assumes that a high pore pressure system locally exists around 30 km depth due to the dehydration derived from facies change in the slab (e.g., Kita et al., 2006; Hasegawa et al., 2007) which has been clearly monitored by tomography studies (e.g., Zhao et al., 2007; Sun et al., 2008; Zhao, 2009; Zhao and Ohtani, 2009-this issue) and geological investigations (e.g., Kutsukake, 2002; see also Mishina, 2009-this issue on resistivity surveys to detect fluid reservoirs). Ariyoshi et al. (2007b) estimate that the value of \( \kappa \) is 0.1 for the deeper part (>30 km depth) on the basis of aseismic propagation speed. Wang and Suyehiro (1999) suggest that the apparent frictional coefficient is about 0.03 from stress field observation in northeastern and southwestern Honshu, Japan, which is consistent with \( \kappa = 0.1 \).

The friction coefficient \( \mu \) in Eq. (1) is assumed to obey a rate- and state-dependent friction law (Dieterich, 1979; Ruina, 1983), as given by

\[ \mu_i = \mu_0 + a \log(V_i / V_0) + b \log(V_i \theta_i / d_i) \tag{3} \]

\[ \frac{d \theta_i}{dt} = 1 - V_i / d_i \tag{4} \]

where \( a \) and \( b \) are friction coefficient parameters, \( d_i \) is the characteristic slip distance associated with \( b, \theta \) is a state variable for the plate interface, \( V \) is slip velocity, and \( \mu_0 \) is a reference friction coefficient defined at a constant reference slip velocity of \( V_0 \).

Eqs. (1), (3), (4) are solved using the Runge–Kutta method with adaptive step-size control (Press et al., 1996). The constant parameters common to all models tested here are: \( C = 30 \text{ GPa}, \beta = 3.75 \text{ km/s}, g = 9.8 \text{ m/s}^2, \rho_{rock} = 2.75 \times 10^3 \text{ kg/m}^3, \rho_w = 1.0 \times 10^3 \text{ kg/m}^3, V_0 = 1 \mu \text{m/s}, \mu_0 = 0.6, \text{ Poisson's ratio } \epsilon = 0.25, \text{ and } V_{pl} = 4.0 \times 10^4 \text{ m/yr or } 1.3 \times 10^{-9} \text{ m/s}.

Frictional stability is usually represented by \( \gamma = a - b \). If \( \gamma > 0 \), frictional stress increases with sliding velocity, similar to viscous coupling. If \( \gamma < 0 \), frictional stress decreases with increasing sliding velocity, resulting in stick-slip behavior (Ruina, 1983). In the present paper, an asperity denotes a region with \( \gamma > 0 \), following Boatwright and Cocco (1996). The plate interface is demarcated into five regions, as shown in Fig. 1b: (i) large asperity (LA) region, (ii) ten middle asperity (MA) regions, (iii) twenty small asperity (SA) regions, (iv) weakly stable region (WS), and (v) strongly stable region (SS). The frictional parameters shown in Fig. 1c are based on rock laboratory results (e.g., Blanpied et al., 1988) \( (a, b, c) = (2.5) \times 10^{-3} \); frictional stability parameters, \( (\gamma_1, \gamma_2, \gamma_3) = (-0.4, 0.01, 4.0) \times 10^{-3} \); and characteristic slip distances, \( (d_1, d_2, d_3) = (40, 10, 0.5) \times 10^{-3} \text{ m} \). The asperity radii take the following values: for LA, \( (R_1, R_2, R_3) = (4.0, 4.5, 5.0) \text{ km} \); for SA, \( (r_1, r_2, r_3) = (2.0, 2.25, 2.5) \text{ km} \); for longer radii of LA, \( (l_1, l_2, l_3) = (90, 95, 100) \text{ km} \) with aspect ratio 0.38. The distance between central points of SA and MA is 5 and 10 km, respectively, so as to be adjacent each SA and MA, which is to be discussed later.

The sizes of the cells \( h_i \) in the asperities are set such that all cells in LA, MA and SA are at least 5.2 times smaller than the critical cell size \( h^c = \eta Gd_i / \gamma (b - a) \), where \( \eta = K_\theta / G \) is a geometrical factor (Rice, 1993). A smaller critical cell size \( l_0 = rGd_i / \eta b \) has been recently proposed on the basis of numerical simulations and analytical results (Rubin and Ampuero, 2005; Perfettini and Ampuero, 2008) and adopted in some simulation studies (e.g., Shibazaki and Shimamoto, 2007; Ziv, 2007). At the center of LA, MA and SA, \( (a_1, \ln a_2, a_3) = (1.6, 5.8, 0.35, 0.31) \text{ and } (0.17, 0.16) \text{ km} \), respectively. Though the cell size of SA along strike and dip direction (0.20, 0.17) \text{ km} \) is slightly larger than \( l_0 \), by reducing the cell size by half we did not find significant qualitative differences in the simulation results discussed next.

3. Simulation results

3.1. Overview of the evolution of stress drop and slip velocity for SA and MA

We uniformly set the initial stress field at the steady state friction value at a rate of 0.9 \( V_{pl} \). Fig. 2 shows (a, c, e, g, i) frictional coefficient (or shear stress normalized by the effective normal stress) and (b, d, f, h, j) slip velocity normalized with respect to \( V_{pl} \) on a common-logarithmic scale averaged in each asperity No. 28–31 (SA) and No. 2–5 (MA) as named in Fig. 1b. The origin time in Fig. 2a–b is one hundred years after the initial conditions, after the first large event of LA. The frequency of slip and stress drop events per decade shown in Fig. 2a–b is about 12–20 for SA and 6–9 for MA, which corresponds to recurrence intervals of 0.5–
0.8 year for SA and 1.1–1.7 years for MA. On the other hand, the recurrence interval of LA is about 180 years.

Since recurrence intervals of SA and MA are short and slip events occur at some asperities most of time, the adaptive time step of the Runge–Kutta method tends to remain small and the computation cost for several slip cycles of LA becomes huge. In this study, we focus mainly on the preseismic stage of LA, where a giant earthquake occurs at LA after 27 years from the end time of Fig. 2a–b, to investigate the stress shadow effect of LA and avoid the heavy calculation cost. In order to validate the simulation results, we performed simulations with different initial conditions and cell sizes and found that our simulation results are not affected by such conditions.

From GPS data analyses for slow slip events in Cascadia, recurrence interval, maximum slip velocity and shear stress drop are estimated to be 14 months ($\text{Miller et al.}, 2002$), 1 m/yr ($3.2 \times 10^{-5} \text{m/s}$) and 0.04–0.06 MPa ($\text{Miyazaki et al.}, 2006$), respectively. In our simulation, the slip velocity averaged in MA and SA is in the range $10^{-10} - 10^{-6} \text{m/s}$ as shown in Fig. 2b, and stress drops of slip events in SA and MA are in the range 0.02–0.08 MPa from Fig. 2a, where the effective normal stress in Eq. (1) at 30 km depth is 51 MPa. These simulation results are quantitatively consistent with the observational results in case of constant stress drop model. Therefore, we basically refer to these slip events in our simulation as slow earthquakes in our simulation. Since the size and frictional properties of asperities are common within the SA and MA groups, the fluctuations of the slow earthquake properties seem to be induced by the interaction between the small asperities (MA and SA).

To examine the interaction processes, we select and investigate four characteristic patterns of slow earthquakes by snapshots of slip velocity in the following sections. Note that some slip events have averaged slip velocities several orders of magnitude greater ($10^{-3} \text{m/s}$), including areas of coseismic slip ($10^{-3} \text{m/s}$), and averaged shear stresses several times greater ($0.16$ MPa) than the observed low-frequency earthquakes and more similar to regular earthquakes. Some other slip events have long duration time than usual low-frequency earthquakes, and are more similar to very low-frequency earthquakes ($\text{Ito et al.}, 2007$; $\text{Ike et al.}, 2007$). Their slip process and propagation speed is similar to one of the following characteristic patterns.

### 3.2. Comparison of propagation process between MA and SA

As an example of chained propagation process of slow earthquakes in MA, Fig. 3 shows a time-series of snapshots of slip velocity normalized by $V_{b}$ on a common-logarithmic scale from 0.16 year in Fig. 2c–d (blue background). It is common in Fig. 3 that small slip events continuously occur above LA. This is due to the shear stress gap derived from shear stress in Eq. (1) between LA($u(t) - 0$) and the outside of trench ($u(t) - V_{g}$; $\text{Savage, 1983}$), and temporally prominent when the distance from the trench to the strongly locked region around LA is short. Therefore, this behavior is artificial. It is needed for our future study to remove the artificial slip behavior by improving our model, though we found that this artificial behavior seems not to affect the character of various types of deep slow earthquakes as seen in Figs. 4–6 explained later.

In Fig. 3, unilateral chained propagation process is clearly seen for MA, with propagation speed between asperities No. 7 to No. 5 of about 0.2 km/day (Fig. 3b–d). In the time span indicated by the blue background in Fig. 2c–d, the patterns of stress drop and averaged slip velocity at asperities No. 3 to 5 appear to be relatively similar but quantitatively different. Especially, the amount of stress drop and averaged slip velocity in asperity No. 3 is greater than in the others. In Fig. 3b–d, there is not only leftward chained propagation from the asperity No. 10 but also rightward propagation from the asperity No. 2, where the latter is much smaller than the former because of the large area locked in the asperity No. 3. In Fig. 3e, both chained propagations cross at the asperity No. 3, which promotes larger stress drop and higher slip velocity. Since similar behavior seems to be seen in the simulation of $\text{Liu and Rice (2005)}$, these results suggest that some phenomena generated by introducing along-strike variations of constitutive parameters or non-uniform initial conditions may be represented by interaction between small asperities.

On the other hand, the propagation process of SA is different from that of MA in some respects. Fig. 4 shows leftward propagation from the asperity No. 2 through No. 31 to No. 22, which is due to the periodic boundary condition. In the time span indicated by a green background in Fig. 2e–f there are two slow earthquakes for each asperity from No. 28 to 31. Propagation speed between asperities No. 31 to 28, No. 28 to 23 and No. 23 to 22 is about 0.2, 0.15 and 0.03 km/day, respectively, which progressively becomes slower than that of MA. Fig. 4e shows that rightward propagation from the asperity No. 27 and 30 is also seen.

These differences from MA are explained as follows. SA has shorter recurrence intervals and smaller moment release because of smaller asperity size with shorter characteristic distance than those of MA. The smaller moment release makes propagation speed slower (0.03 km/day for SA is smaller than 0.2 km/day for LA), which causes that recurrence interval of SA is relatively much shorter than the MA. Since the passage time of aseismic slip across more than twice the SA diameters (10 km), in addition, locking of SA soon after the occurrence of slow earthquakes, due to their short characteristic distance, tends to prevent aseismic slip propagation. Therefore, slow earthquakes occur again soon after the passage of aseismic slip from asperity No. 29 as shown in Fig. 2e–f. This is why propagation process of SA as shown in Fig. 4e–f appears to be bilateral, rather than the unilateral propagation seen in Fig. 3.

#### 3.3. Physical process of multiple ruptures and very low-frequency earthquake

Fig. 5 shows an example of a multi rupture process between asperities No. 3 to 5 in the time span indicated by a pink background in Fig. 2i–b. (ii) The velocity of preslip becomes locally higher (nearly red) around the center of asperity No. 5 and in the frictionally unstable region ($\gamma<0$) between the centers of asperities No. 4 and 5 (Fig. 5c). (iii) A slow earthquake occurs in asperity No. 5 (Fig. 5d), and (iv) asperity No. 4 follows (Fig. 5e). (v) Afterslip of MA has enclosed the three asperities No. 3 to 5 (Fig. 5f). From Fig. 5d–e, the rupture speed from asperity No. 3 to 4 is roughly 3 km/day, which is significantly faster than that of Figs. 3 and 4. Slip propagation is promoted by the preslip of the slow earthquakes (warm colors in Fig. 5d–e) that has covered the area between the two asperities No. 3 and 4 in the dip range of 110–120 km. Therefore, a necessary condition for this multiple rupture is such synchronized preslip stage of slow earthquakes on each asperity as shown in Fig. 5b.

The series of snapshots in Fig. 6 show a case with no synchronization. Fig. 6a shows a pair of slow earthquakes at asperities No. 5 and 7, while Fig. 6b–c shows a pair at asperities No. 4 and 6. After that, a slow
earthquake occurs on asperity No. 3 (Fig. 6e), then slip propagates to the next asperity, No. 4 (Fig. 6f). In the time span indicated by a yellow background in Fig. 2g–h, some slow earthquakes with averaged slip velocities nearly as low as $V_{pl}$ have occurred at asperity No. 4, after the time of Fig. 6a, which is due to the short time for shear stress healing as shown in the friction history of Fig. 2g. This simulation result may
Fig. 2 (continued).
explain the physical process of very low-frequency earthquake generation.

4. Summary and discussion

Our simulation represents various types of slow earthquakes, including low-frequency earthquakes and very low-frequency earth-
quakes, due to interaction of asperities aligned along the strike direction, with same size and frictional properties. This result indicates that the interaction between asperities may be a possible mechanism for the generation of low-frequency earthquake and very low-frequency earthquake in the same fault region, without requiring different asperity sizes as previously proposed (Ito et al., 2007).

Fig. 3. Snapshots of slip velocity from time 0.16 year as marked by blue color in Fig. 2a–d. Italic numbers under MA are identification of asperities.
Moreover, our simulation also shows unilateral/bilateral propagation and multiple rupture process. We also performed models with longer distance between asperities (more than 5 km for SA and 7.5 km for MA) and found that most of slow earthquakes occurred independently and had weaker variability of slip velocity and stress drop. These results suggest that the interaction effect may be a possible mechanism of low-frequency earthquake migration, alternative to the fluid movement hypothesis (Obara, 2002), and that the distribution of asperities may be very dense along the strike direction at the depth of around 30 km.

The propagation speed in our model varies in the range 0.03–3 km/day, which is more dispersed than observational results in the range 5–15 km/day (Obara, 2002; Rogers and Dragert, 2003; Obara and Hirose, 2006). Since the propagation speed in our model is

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**Fig. 4.** Snapshots of slip velocity from time 25.0 years as marked by green color in Fig. 2a–b, e–f. Italic numbers under SA are identification of asperities.
significantly lower than observed, it is necessary for us to explain the propagation speed quantitatively by modifying our model. Ariyoshi et al. (2007b) demonstrated that shorter characteristic distance as well as lower effective normal stress makes afterslip propagation of a large earthquake faster by changing frictional property. However, models with shorter characteristic distance than the original model in Fig. 1 need heavier computations, especially just before and after giant earthquakes at LA.

From Fig. 2a–b, the recurrence intervals of SA and MA tend to be shorter because slip velocity field around LA becomes higher towards to the preseismic stage of LA in comparison with Figs. 3–6. Ariyoshi et al. (2007a) found that slow earthquakes occur at a
small asperity in the passage of large postseismic slip, which could be another mechanism of very low-frequency earthquake generation. It is our future study to improve our numerical simulations so as to explain the propagation speed quantitatively and to investigate the change of slow earthquake behavior before and after giant earthquakes in order to find a way to monitor the state of large asperities.

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